

I'm not robot!

Determine what type of sequence it is (arithmetic, geometric, linear, quadratic, cubic, or quartic). Give the n th term and value for the specified term.

1	2	3	4	5	6	n	10
40	63	90	121	156	195		

$(2n+3)(n+7)$
 $(2(10)+3)(10+7)$
 $23(17)$
 $= 391$

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1	2	3	4	5	6		
1	2	3	4	5	6	n	20
1	2	3	4	5	6		

$T_n = 7 \cdot (n-1)^{n-1}$
 $T_n = 4(-3)^{n-1}$
 $T_9 = 4(-3)^{8-1}$
 $= 26244$

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 $= 26244$

Determine if the sequence is linear, quadratic, cubic, or quartic.

1	2	3	4	5	6	n	20
1	2	3	4	5	6		
1	2	3	4	5	6	n	20
1	2	3	4	5	6		

$T_n = 7 \cdot (n-1)^{n-1}$
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Find the arithmetic mean of 12 and 48.

$$\frac{12+48}{2} = \frac{60}{2} = 30$$

Find the geometric mean of 3 and 27.

$$\sqrt{3 \cdot 27} = \sqrt{81} = 9$$

Expand $(2a + b)^5$

$$\binom{5}{0} 2^5 a^5 b^0 + \binom{5}{1} 2^4 a^4 b^1 + \binom{5}{2} 2^3 a^3 b^2 + \binom{5}{3} 2^2 a^2 b^3 + \binom{5}{4} 2 a^1 b^4 + \binom{5}{5} a^0 b^5$$

$$32a^5 + 80a^4b + 80a^3b^2 + 40a^2b^3 + 10ab^4 + b^5$$

5. Here are the first three figures of a pattern.

Figure 1: 4 segments
 Figure 2: 12 segments
 Figure 3: 24 segments

Arithmetic

a. List the number of line segments in Figures 1-7.
 $u_1=4, u_2=12, u_3=24, u_4=40, u_5=60, u_6=84, u_7=112$

b. Write a recursive formula that generates the sequence you found in part a.
 $u_n = u_{n-1} + 8n - 4$ or $u_n = 8n - 4$

c. Write an explicit formula that generates the sequence you found in part a.
 $u_n = 4n^2$

d. How many line segments are in Figure 20?
 $u_{20} = 4(20)^2 = 1600$

e. Which figure has 144 line segments?
 $144 = 4n^2 \Rightarrow n^2 = 36 \Rightarrow n = 6$

Geometric

6. Consider the sequence 0.05, 0.15, 0.45, 1.35, 4.05, ...

a. Write a recursive formula for the sequence. Use u_1 to represent the starting term.
 $u_n = 3u_{n-1}$ or $u_n = 0.05 \cdot 3^n$

b. Write an explicit formula for the sequence.
 $u_n = 0.05 \cdot 3^{n-1}$ or $u_n = 0.15 \cdot 3^{n-2}$

c. What is the 7th term of the sequence?
 $u_7 = 0.05 \cdot 3^6 = 1.215$

d. Which term of the sequence is the first to be greater than 20,000?
 $20,000 < 0.05 \cdot 3^n \Rightarrow 400,000 < 3^n \Rightarrow n > \log_3(400,000) \approx 12.8$
 The 13th term is the first to be greater than 20,000.

7. Write an equation to define the sequence u_n graphed below.

$u_n = 3n - 2$

Name : _____ Score : _____
 Teacher : _____ Date : _____

Arithmetic Sequences

Determine whether each sequence is arithmetic. If so, find the common difference.

- 1) 15.2, 8.5, 1.8, -4.9 ...
- 2) 8.4, 16.1, 23.8, 31.5 ...
- 3) 5.1, -0.8, -6.7, -12.6 ...
- 4) 14.3, 20.3, 26.3, 32.3 ...

Find the first four terms and stated term given the arithmetic sequence, with a_1 as the 1st term.

- 5) $a_n = 25.5 - 6.8n, a_{10}$
- 6) $a_n = 25 - 10n, a_5$
- 7) $a_n = 11 + 9n, a_6$
- 8) $a_n = 65 - 35n, a_8$

Given the first term and common difference, find the first four terms and the formula.

- 9) $a_1 = 25, d = 100$
- 10) $a_1 = 5, d = 5$
- 11) $a_1 = 24, d = -15$
- 12) $a_1 = 9, d = -50$

